

Mathematics (MATH)

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The Department of Mathematics offers a major that can satisfy a variety of student interests. By proper choice of electives, students whose major is mathematics can prepare themselves for graduate study in mathematics or related areas, for the teaching of mathematics at the secondary school level, for professional school in law or health science, or for the application of mathematics in science, business and industry.

Students majoring in mathematics generally will have a number of elective courses and are encouraged to use these electives to broaden their background in mathematics or in a related area of special interest. The department suggests that courses in biology, business administration, chemistry, economics, geology, physics, psychology and quantitative methods/computer science are especially appropriate.

If students have not already made a choice of language, the department suggests that particularly valuable languages in the study of mathematics are French, German and Russian.

The department also has a major for students pursuing careers in actuarial science. See listing under Actuarial Science in this catalog.

Students should see the chair of the Department of Mathematics for advice in selecting courses for a particular purpose.

Center for Applied Mathematics

Within the Department of Mathematics, the Center for Applied Mathematics provides opportunities for students to work on significant mathematical problems of current interest to business, industry, and government.

Major in Mathematics

All majors must complete the following courses:

- 113 Calculus I (or 108-109)
- 114 Calculus II
- 200 Multi-Variable Calculus
- 210 Linear Algebra and Differential Equations
- 317 Real Analysis

Allied requirements:

One of:

- QMCS 130 Problem Solving in the Natural Sciences
- or*
- QMCS 237 Software Design Using Scientific Languages

Plus one of the following sequences:

- ECON 351-352-418
- PHYS 111-112
- QMCS 410-411

or a total of 44 credits in mathematics including one of the following sequences:

- MATH 313-314
- MATH 315-316
- MATH 325-450

(to complete a pure mathematics program, a student should choose one of 301, 310, at least one of 302, 309, 385, 400, 419, 420, and two additional courses numbered 300 or above;

to complete an applied mathematics program, a student should choose 300, 310, 315, 316, plus one of 303, 313, and at least one of 385, 419;

to complete a statistics program, a student should choose 310, 313, 314, 333, 385 and one additional course)

In addition to other requirements, a student must successfully complete at least 16 credits in mathematics courses numbered 300 and above at the University of St. Thomas.

Teacher Licensure in Mathematics

See Department of Teacher Education

Mathematics

Minor in Mathematics

A minor in mathematics is available to support majors in many other departments.

A total of twenty-four credits including:

113 Calculus I (or 108-109)

114 Calculus II

Plus at least one of:

200 Multi-Variable Calculus

210 Linear Algebra and Differential Equations

Plus:

At least twelve additional credits in courses numbered above 200 (or approved by the department chair).

To qualify for a minor in mathematics, in addition to other requirements, a student must successfully complete at least three courses (12 semester credits) in mathematics numbered 200 and above at the University of St. Thomas.

005 Basic Math Skills

0 credit

This review of arithmetic and elementary algebra is designed to prepare the student to study MATH 100 (Mathematical Sampler) or MATH 101 (Finite Mathematics). The course is designed as a self-directed study experience, with lectures scheduled only during the J-term and summer offerings. The student will have access to textbook explanations and exercises, videos, CD-ROMs and tutors to gain mastery of the material. Appropriate testing is done with the tutors in the Mathematics Resource Center (MaRC). A nominal registration fee is charged.

100 Mathematical Sampler

This survey of basic mathematical concepts includes both modern and historical perspectives. Emphasis is on the development and appreciation of mathematical ideas and their relationship to other disciplines. Topics include, among others: mathematical problem-solving; sets; an introduction to randomness, probability and statistics (through application of the normal distribution); historical systems of numeration; mathematical techniques of counting (multiplication principle, Venn and tree diagrams, etc.); coordinate geometry; simple transformations; and patterns of symmetry. This course satisfies the general requirement for a course in mathematics and is also recommended as a first course in mathematics for prospective elementary teachers.

Prerequisite: A satisfactory score on the mathematics placement exam

101 Finite Mathematics

Elementary set theory, linear equations and matrices, linear programming, finite probability, applications primarily in business and the social sciences.

Prerequisite: A satisfactory score on the mathematics placement examination

105 Precalculus (108, 109)

The real numbers; basic algebra; analytical treatment of the elementary functions emphasizing the exponential, logarithmic and trigonometric functions and their graphs. (This course is intended as preparation for 113 and does not fulfill a general graduation requirement.)

Prerequisite: A satisfactory score on the mathematics placement examination

108 Calculus With Review I (105, 111, 113)

The first course of a two-course sequence designed to integrate introductory calculus material with the algebraic and trigonometric topics necessary to support that study. Review topics include: number systems, basic algebra, functions, the Cartesian coordinate system, graphing and inverse functions. Calculus topics include limits, continuity, derivatives for algebraic functions, applications of derivatives and more graphing. This course is intended only for students planning to take 109 and does not satisfy a general requirement.

Prerequisite: A satisfactory score on the mathematics placement examination

109 Calculus With Review II (105, 111, 113)

The second course of a two-course sequence designed to integrate introductory calculus material with the algebraic and trigonometric topics necessary to support that study. Review topics include: exponential and logarithmic functions, trigonometric functions and their inverses and associated graphs. Calculus topics include: derivatives of the transcendental functions, applications of those derivatives and an introduction to integration.

Prerequisite: a grade of C- or better in 108

111 Calculus for Business and Social Science (108, 109, 113)

An introductory course in calculus with motivation and examples drawn from business and the social sciences whenever possible. Does not include the calculus of trigonometric functions.

Prerequisite: a grade of C- or above in 105 or a satisfactory score on the mathematics placement examination. (Four years of high school mathematics, including college algebra, also are recom-

mended as background for this course.) Students intending to continue in calculus are strongly advised to take 113.

113 Calculus I (108, 109, 111)

An introductory course in calculus: limits; derivatives and integrals of algebraic, exponential, logarithmic and trigonometric functions of one real variable; applications primarily in the natural sciences. This course fulfills the second-level Computer Competency requirement in the core curriculum.

Prerequisite: a grade of C- or above in 105 or a satisfactory score on the mathematics placement examination. (Four years of high school mathematics, including college algebra and trigonometry, also are recommended as background for this course.)

114 Calculus II

Techniques of integration; applications of integration; infinite series; L'Hospital's rule; improper integrals; an introduction to vectors. This course fulfills the second-level Computer Competency requirement in the core curriculum.

Prerequisite: a grade of C- or above in 113 or 109 (or 111, with permission of the department chair)

121 Structures of Elementary Mathematics

An examination of the mathematical underpinnings of the elementary school curriculum with an emphasis on the understanding of mathematical concepts. Topics will include foundations of integer and rational arithmetic, notions of place-value and base, number sense and estimation, functions and their applications, Euclidean geometry, regular polygons and polyhedra, concepts of symmetry, analysis and classification of patterns, mathematics of measurement, the use of models, the role of logic in mathematical discourse, applications of statistics in the schools, and mathematical connections to other disciplines. The LOGO computing language is used to explore mathematical topics.

Prerequisites: 100 and QMCS 120

128 Introduction to Discrete Mathematics

A survey of basic discrete mathematical concepts. Topics include: Boolean algebra, logic, analysis of algorithms, mathematical induction and matrices. Focus on applications to computer science. (This course is a prerequisite for QMCS 240.)

Prerequisite: 111 or 113 or 109 (may be taken concurrently with consent of the instructor)

200 Multi-Variable Calculus

Vector algebra in two and three dimensions, partial derivatives, multiple integrals, line integrals, surface integrals, Green's Theorem, Stoke's Theorem, divergence theorem. This course fulfills the second-level Computer Competency requirement in the core curriculum.

Prerequisite: a grade of C- or higher in 114

210 Linear Algebra and Differential Equations

The course will introduce the student to linear algebra, differential equations and applications of linear algebra to differential equations. Topics to be covered will include: vector spaces, matrices, determinants, eigenvalues and eigenvectors, linear transformations, systems of ordinary differential equations, Laplace transform, series solutions to selected differential equations, and applications to engineering. This course fulfills the second-level Computer Competency requirement in the core curriculum.

Prerequisite: a grade of C- or higher in 114

264 The Mathematical Theory of Interest

A survey of topics in the mathematical analysis of financial transactions which involve payments made over time. Specific areas of concentration will include the time value of money; the analysis of annuities; amortization and sinking funds; and the pricing and rates of return on investments. Both continuous time and discrete time problems will be considered.

Prerequisite: 200 or permission of the instructor

295, 296, 297, 298 Topics

The subject matter of these courses, announced in the annual *Class Schedule*, will vary from year to year, but will not duplicate existing courses. See the description of these courses at the beginning of the "Departments and Curricula" section of this catalog.

300 Differential Equations and Applied Mathematics

Linear ordinary differential equations and systems; standard methods of solution; Laplace transforms; series solution; introduction to nonlinear differential equations and dynamical systems. Models and applications in the physical, biological, behavioral, and social sciences.

Prerequisite: 200 and 210 or permission of the department chair

301 Abstract Algebra I

Properties of sets, relations and mappings; introduction to groups, rings and fields. Offered in fall semester.

Prerequisite: 210

Mathematics

302 Abstract Algebra II

Topics in modern algebra with applications. Includes material selected from the theory of groups, rings, and fields; linear algebra; Boolean algebra and discrete structures. Offered in spring semester of even-numbered years.

Prerequisite: 301

303 Statistics for the Applied Sciences (313, 314)

Probability, Estimation, Hypothesis Testing, Analysis of Variance, Regression Analysis, Topics selected from Experimental Design, Statistical Process Control, Non-Parametric Methods, Factor Analysis as time permits. This course fulfills the second-level Computer Competency requirement in the core curriculum.

Prerequisite: 200

309 Discrete Mathematical Structures

An introduction to topics in discrete mathematics with applications, primarily to computer science. Topics include sets, counting, matrices, algorithms, graph theory, semigroups, logic and Boolean algebras, finite state machines and Turing machines. Offered in spring semester of odd-numbered years.

Prerequisite: programming experience and 301 or instructor's permission

310 Modern Linear Algebra

Linear algebra and applications. Topics include linear equations, matrix theory, linear spaces, linear mappings, canonical forms, and inner product spaces. Applications chosen from such topics as numerical linear algebra, least squares, hermitian and positive definite matrices, and electrical networks.

Prerequisite: 210

313 Probability (303)

Probability theory in discrete and continuous sample spaces; random variables and distribution functions; moments; the moment-generating function; functions of random variables; law of large numbers; central limit theorem. This course fulfills the second-level Computer Competency requirement in the core curriculum. Offered in fall semester.

Prerequisite: 200 and 210

314 Mathematical Statistics (303)

Populations and random sampling; sampling distributions. Theory of statistical estimation; criteria and methods of point and interval estimation. Theory of testing statistical hypotheses; non-parametric methods. Offered in spring semester.

Prerequisite: 313

315, 316 Applied Mathematics and Modeling

These are related but unsequenced courses offered through the Center for Applied Mathematics (CAM). Course content will be drawn from areas of applied mathematics, including: mathematical analysis of data, database theory, discrete and continuous modeling, simulation, applied statistics, coding theory, expert systems, neural network analysis, signal processing and optimization theory. Students will work in teams on projects of current interest to local industry, business and government organizations.

Prerequisite: 200 and 210

317 Real Analysis

Topology of the real numbers. Functions of one real variable. Rigorous development of continuity and uniform continuity; differentiability; uniform convergence. Sequences and series. Offered fall semester.

Prerequisite: 200 and 210

325 Geometry

Axioms for geometries; geometrical transformations and their invariants; non-Euclidean geometries; additional topics. Offered in spring semester.

Prerequisite: 200 and 210 or permission of the instructor

333 Applied Statistical Methods: Regression, Time Series, Forecasting

Regression and exponential smoothing methods; Stochastic Time Series: auto- and cross-correlation, autoregressive moving average models; application to forecasting.

Prerequisite: 314

385 Mathematical Methods of Numerical Analysis

Rigorous mathematical treatment of standard topics in numerical analysis including solutions to linear and nonlinear systems, interpolation, numerical integration and differentiation, differential equations, and iterative techniques in matrix algebra. This course provides a theoretical foundation for the numerical solution of mathematical problems. Offered in spring semester.

Prerequisite: 317 and QMCS 130 or QMCS 237 or permission of instructor

Modern and Classical Languages

400 Dynamical Systems and Chaos

An introduction to discrete and continuous dynamical systems and applications with topics including: iterated mappings in one and two dimensions, phase-plane theory, nonlinear differential equations, and chaos. Additional topics will be chosen from among bifurcations, stability, attractors, Lyapunov functions, Julia sets and Mandelbrot sets.

Prerequisite: 300 or 317 or permission of instructor

419 Complex Variables

Analytic functions; theorems of Cauchy; Laurent series; residue calculus; entire and meromorphic functions; conformal mapping.

Prerequisite: 317

420 Topology

Properties of Euclidean spaces; general spaces; mappings; separation properties; connectedness; compactness; metrizable spaces.

Prerequisite: 317

450 Advanced Mathematics from an Elementary Point of View

This course gives students a sense of the history, applicability and currency of one or more mathematical ideas and serves as a capstone mathematics course for students seeking to teach secondary mathematics. In the course, students make substantial oral and written presentations on topics carefully selected to have a strong relationship to secondary school mathematics. They use publications, e.g. The American Mathematical Monthly, Mathematics Magazine, Mathematical Intelligencer and Scientific American, as well as standard texts, as sources for their work.

Prerequisite: 301 and 317, senior or graduate standing and declared intent to complete secondary licensure in mathematics. Other students having the course prerequisites may be admitted, but it is their responsibility to determine the relationship of this course to their program of study

475, 476, 477, 478 Experiential Learning

See the description of these courses at the beginning of the “Departments and Curricula” section of this catalog.

483, 484, 485, 486 Seminar

See the description of these courses at the beginning of the “Departments and Curricula” section of this catalog.

487, 488, 489, 490 Topics

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491, 492, 493, 494 Research

See the description of these courses at the beginning of the “Departments and Curricula” section of this catalog.

495, 496, 497, 498 Individual Study

See the description of these courses at the beginning of the “Departments and Curricula” section of this catalog.

Media Studies

See Department of Journalism and Mass Communication.

Modern and Classical Languages

Moorman (chair), Badessich, Dziekowicz, Federico, Feigenbaum, Heberlein, Hundley, Martín-Morán, Raschio, Sandmann, Schons, Shambour, Wolsey, Gochberg*, Richmond*

The Department of Modern and Classical Languages offers major and minor concentrations in classical languages, French, German, Latin and Spanish, with additional minors in Greek and Japanese. A Russian major and minor and a Japanese major are available through the Associated Colleges of the Twin Cities. In cooperation with the ACTC, courses also are available in Chinese and Italian.

The department also offers major concentrations in language with business (international business – language intensive) and language with English (literary studies).

National Collegiate Foreign Language Honor Society

Alpha Mu Gamma, the National Collegiate Foreign Language Honor Society, was organized at St. Thomas in 1980. The aims of the society are to recognize achievement in the field of foreign language study and to encourage an interest in the study of foreign languages, literatures and civilizations.